

1. Octane ( $C_8H_{18}$ ) is a main component of gasoline used in cars.

A) Write a balanced chemical equation for the combustion of octane with oxygen.



B) Using the following standard enthalpies of formation, determine the standard change in enthalpy ( $\Delta H_{rxn}^{\circ}$ ) for the combustion reaction of octane.

$$\Delta H_f^{\circ}[C_8H_{18} (l)] = -249.9 \frac{\text{kJ}}{\text{mol}} \quad \Delta H_f^{\circ}[CO_2 (g)] = -393.5 \frac{\text{kJ}}{\text{mol}} \quad \Delta H_f^{\circ}[H_2O (g)] = -241.8 \frac{\text{kJ}}{\text{mol}}$$

$$\begin{aligned}\Delta H_{rxn}^{\circ} &= n_{CO_2} \Delta H_f^{\circ}(CO_2) + n_{H_2O} \Delta H_f^{\circ}(H_2O) - n_{C_8H_{18}} \Delta H_f^{\circ}(C_8H_{18}) - n_{O_2} \Delta H_f^{\circ}(O_2) \\ &= 16 \text{ mol} \left( -393.5 \frac{\text{kJ}}{\text{mol}} \right) + 18 \text{ mol} \left( -241.8 \frac{\text{kJ}}{\text{mol}} \right) - 2 \text{ mol} \left( -249.9 \frac{\text{kJ}}{\text{mol}} \right) - 25 \text{ mol} \left( 0 \frac{\text{kJ}}{\text{mol}} \right) \\ \Delta H_{rxn}^{\circ} &= -10148.6 \text{ kJ}\end{aligned}$$

C) How much  $CO_2$  gas is produced if 1.25 L of octane (density 0.703 g/mL) are combusted?

$$1.25 \text{ L } C_8H_{18} \times \frac{1000 \text{ mL}}{1 \text{ L}} \times \frac{0.703 \text{ g}}{1 \text{ mL}} = 878.8 \text{ g } C_8H_{18}$$

$$878.8 \text{ g } C_8H_{18} \times \frac{1 \text{ mol}}{114.22 \text{ g}} = 7.69_3 \text{ mol } C_8H_{18}$$

$$7.69_3 \text{ mol } C_8H_{18} \times \frac{16 \text{ mol } CO_2}{2 \text{ mol } C_8H_{18}} \times \frac{44.01 \text{ g } CO_2}{1 \text{ mol } CO_2} = 2710 \text{ g } CO_2$$

2. A total of 1411 kJ of heat is applied to 500. mL of liquid water, originally 25.0 °C, to convert it all to water vapor. What is the final temperature of the gaseous water?

$$c_P[H_2O(s)] = 37.1 \frac{\text{J}}{\text{mol} \cdot \text{°C}}$$

$$\Delta H_{fus}[H_2O] = 6.01 \frac{\text{kJ}}{\text{mol}}$$

$$c_P[H_2O(l)] = 75.3 \frac{\text{J}}{\text{mol} \cdot \text{°C}}$$

$$\Delta H_{vap}[H_2O] = 40.67 \frac{\text{kJ}}{\text{mol}}$$

$$c_P[H_2O(g)] = 33.6 \frac{\text{J}}{\text{mol} \cdot \text{°C}}$$

First, determine the amount of  $H_2O (l)$  using its density and molar mass:

$$500. \text{ mL } H_2O \times \frac{1 \text{ g}}{1 \text{ mL}} \times \frac{1 \text{ mol } H_2O}{18.02 \text{ g } H_2O} = 27.7_5 \text{ mol } H_2O$$

Second, determine how much heat is required to heat  $H_2O (l)$  from 25.0 °C to 100.0 °C:

$$q_{\text{liquid}} = nc_P\Delta T = (27.7_5 \text{ mol}) \left( 75.3 \frac{\text{J}}{\text{mol} \cdot \text{°C}} \right) (100.0 \text{ °C} - 25.0 \text{ °C}) = 156700 \text{ J} = 156.7 \text{ kJ}$$

Third, determine how much heat is required to vaporize  $H_2O (l)$  to  $H_2O (g)$ :

$$q_{\text{vap}} = n\Delta H_{\text{vap}} = (27.7_5 \text{ mol})(40.67 \text{ kJ}) = 1128.6 \text{ kJ}$$

Fourth, realize that we will heat the  $H_2O (g)$  after the vaporization process ( $q_{\text{gas}}$ ), so:

$$q_{\text{total}} = q_{\text{liquid}} + q_{\text{vap}} + q_{\text{gas}}$$

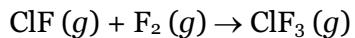
$$q_{\text{gas}} = q_{\text{total}} - q_{\text{liquid}} - q_{\text{vap}} = 1411 \text{ kJ} - 156.7 \text{ kJ} - 1128.6 \text{ kJ} = 126 \text{ kJ}$$

Lastly, determine the final temperature of the  $H_2O (g)$  from heating with 126 kJ heat:

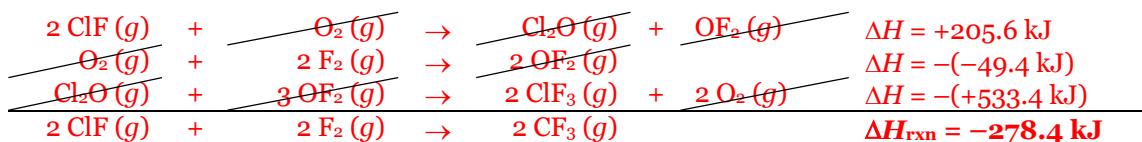
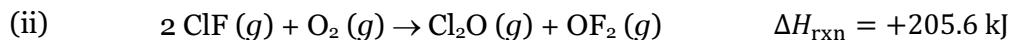
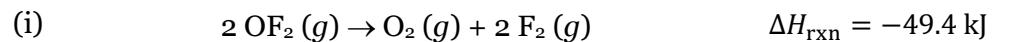
$$q_{\text{gas}} = nc_P\Delta T \rightarrow T_{\text{final}} - T_{\text{initial}} = \frac{q_{\text{gas}}}{nc_P}$$

$$T_{\text{final}} = \frac{126 \text{ kJ} \times \frac{1000 \text{ J}}{1 \text{ kJ}}}{(27.7_5 \text{ mol}) \left( 33.6 \frac{\text{J}}{\text{mol} \cdot \text{°C}} \right)} + 100^\circ\text{C} = 230^\circ\text{C}$$

3. Consider the following reaction:



Calculate  $\Delta H_{\text{rxn}}$  for the above reaction given the following reactions.



But we need to divide the entire equation by 2, so  $\Delta H_{\text{rxn}} = -139.2 \text{ kJ}$ .