

# Heating Curves

**DR. MIOY T. HUYNH**  
YALE UNIVERSITY  
CHEMISTRY 161  
FALL 2019

[www.mioy.org/chem161](http://www.mioy.org/chem161)

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

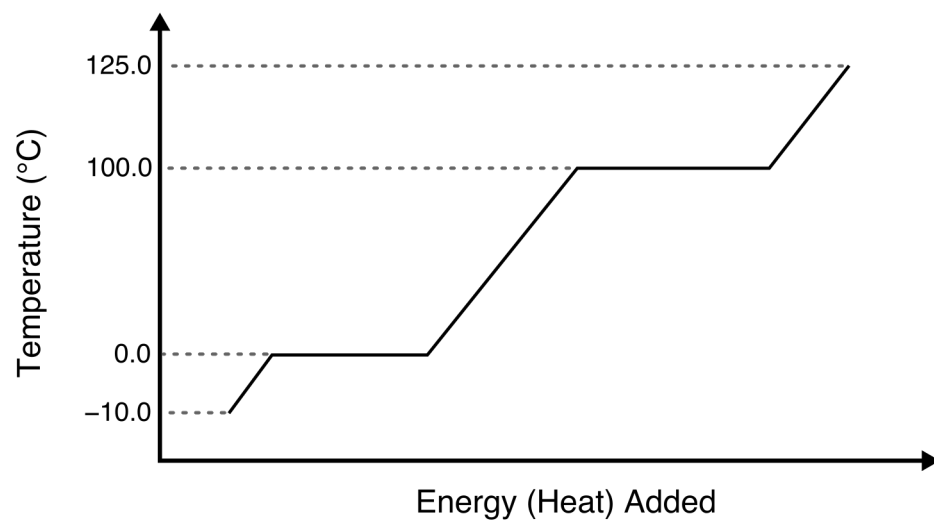
How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



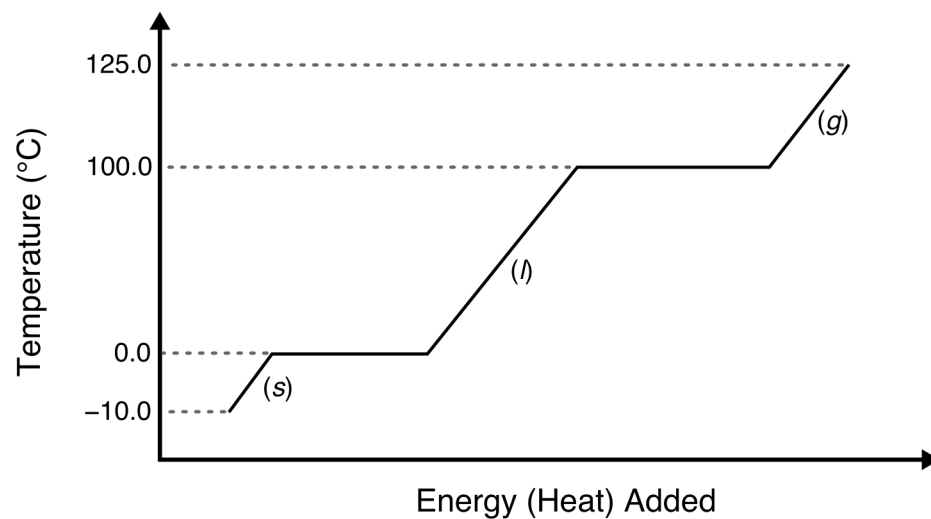
## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:

The **sloped** regions are heating of a particular phase.



## A Guided Example

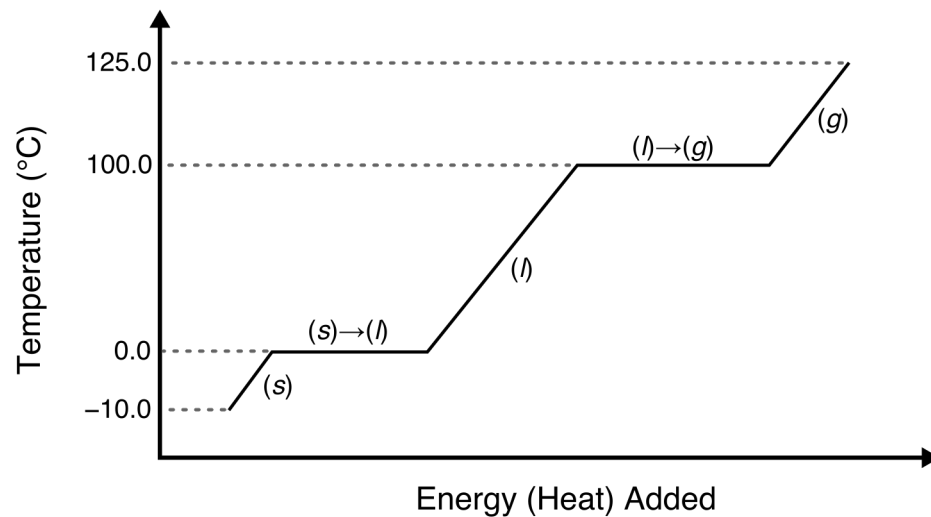
Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:

The sloped regions are heating of a particular phase.

The **horizontal** regions are where we change phases.



## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

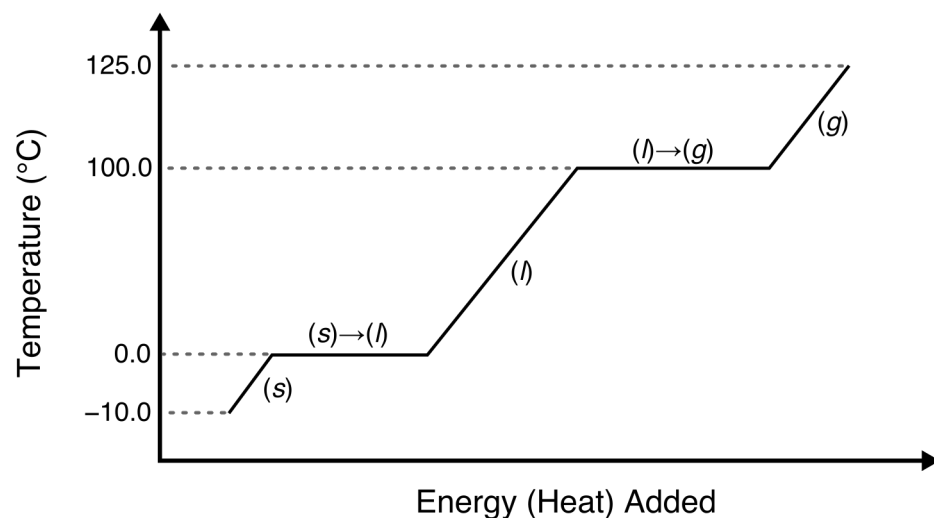
How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:

The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

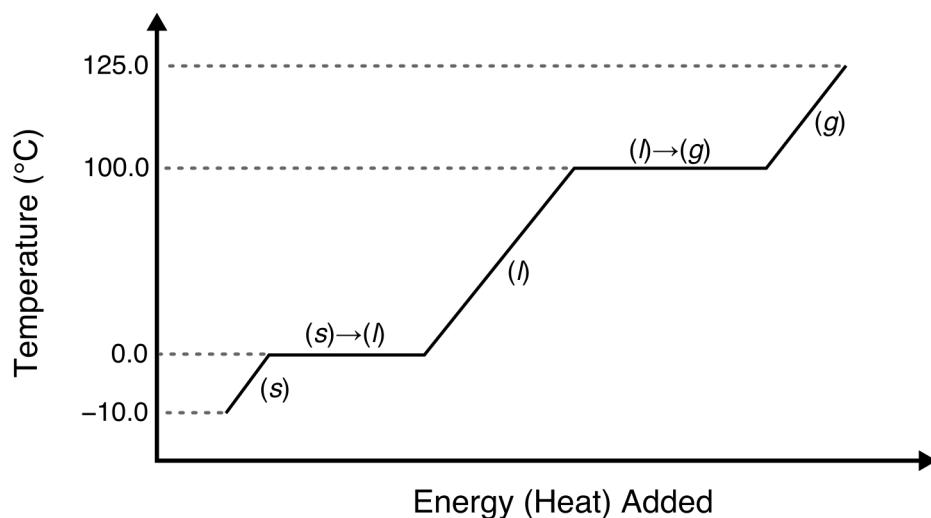


## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

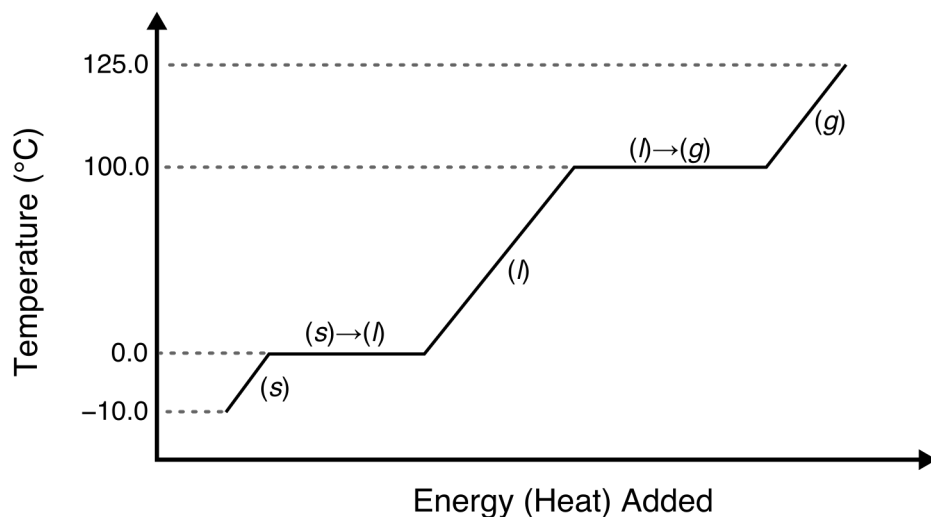
- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$

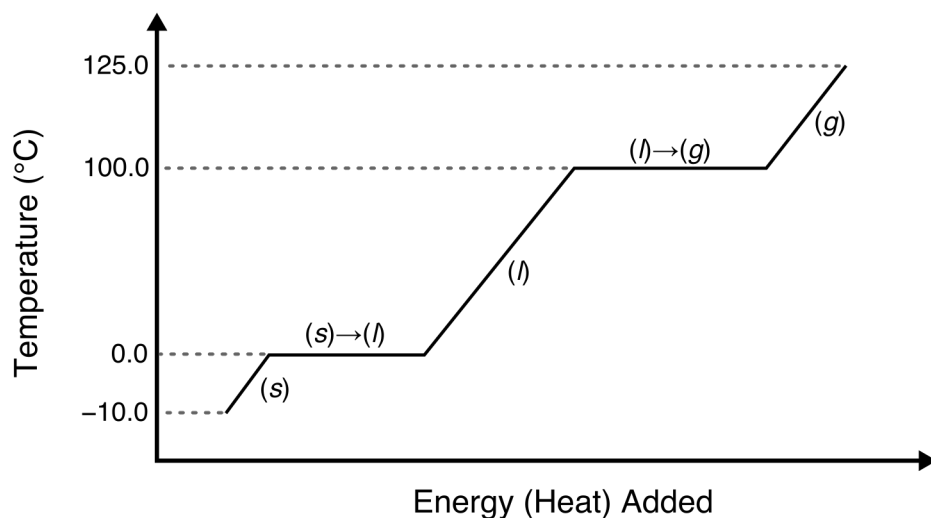


## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

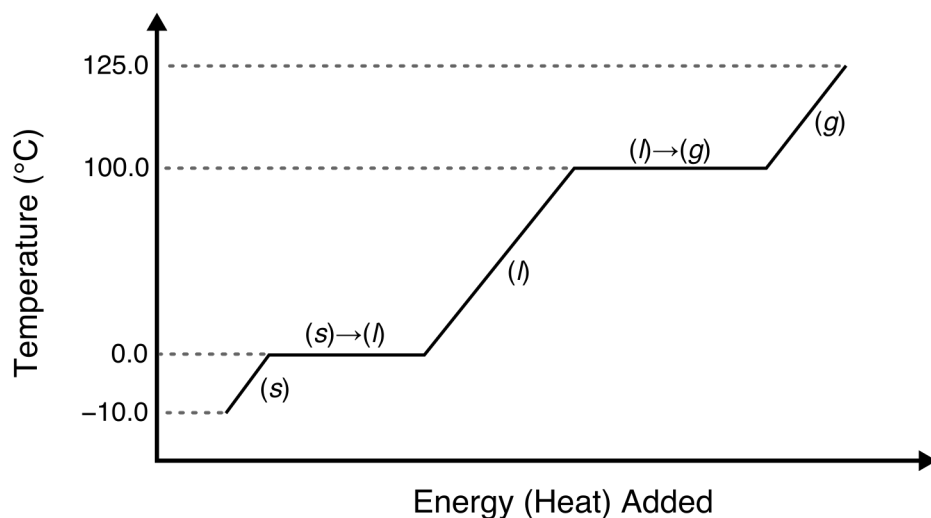
- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

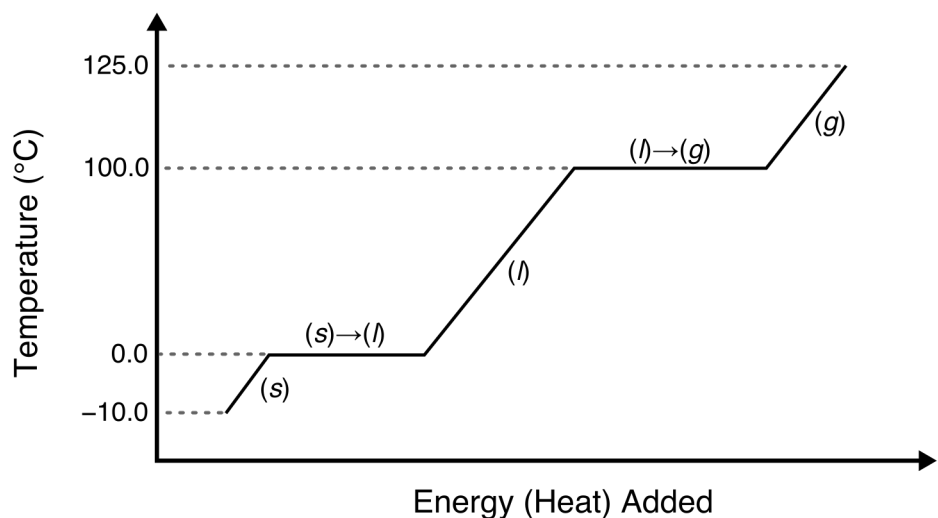
- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$
- $q_4$  = changing all water to vapor at  $100.0\text{ }^{\circ}\text{C}$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

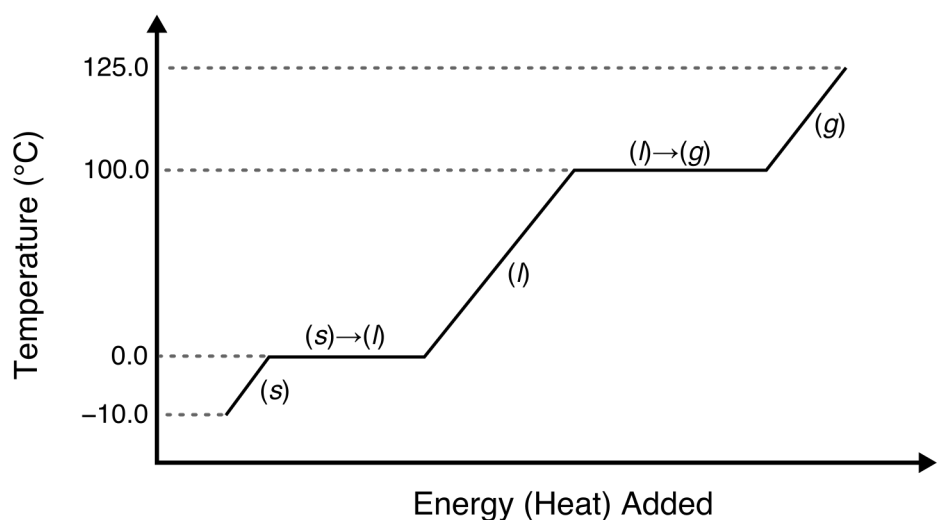
- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$
- $q_4$  = changing all water to vapor at  $100.0\text{ }^{\circ}\text{C}$
- $q_5$  = heating vapor from  $100.0\text{ }^{\circ}\text{C}$  to  $125.0\text{ }^{\circ}\text{C}$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.  
The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$
- $q_4$  = changing all water to vapor at  $100.0\text{ }^{\circ}\text{C}$
- $q_5$  = heating vapor from  $100.0\text{ }^{\circ}\text{C}$  to  $125.0\text{ }^{\circ}\text{C}$

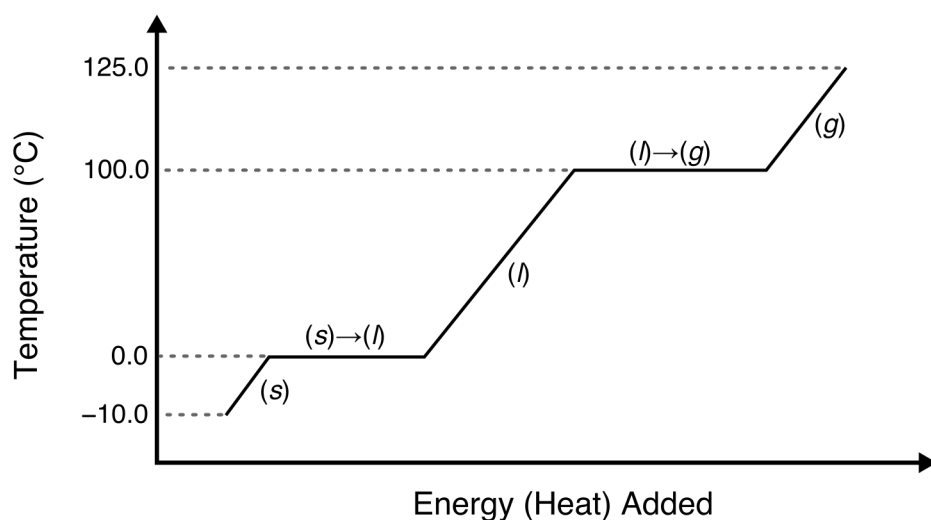
*Let's determine each of these  $q$  values one by one.*

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$

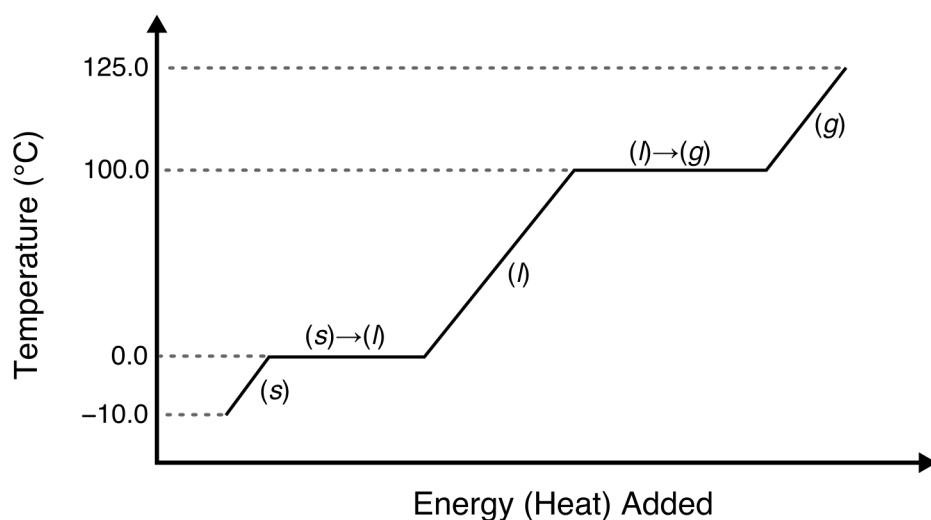
$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$

$$q_1 = n c_p \Delta T$$

$$= (0.277_5 \text{ mol}) \left( 37.1 \frac{\text{J}}{\text{mol} \cdot ^{\circ}\text{C}} \right) (0.0\text{ }^{\circ}\text{C} - (-10.0\text{ }^{\circ}\text{C}))$$

$$q_1 = 102.9 \text{ J}$$

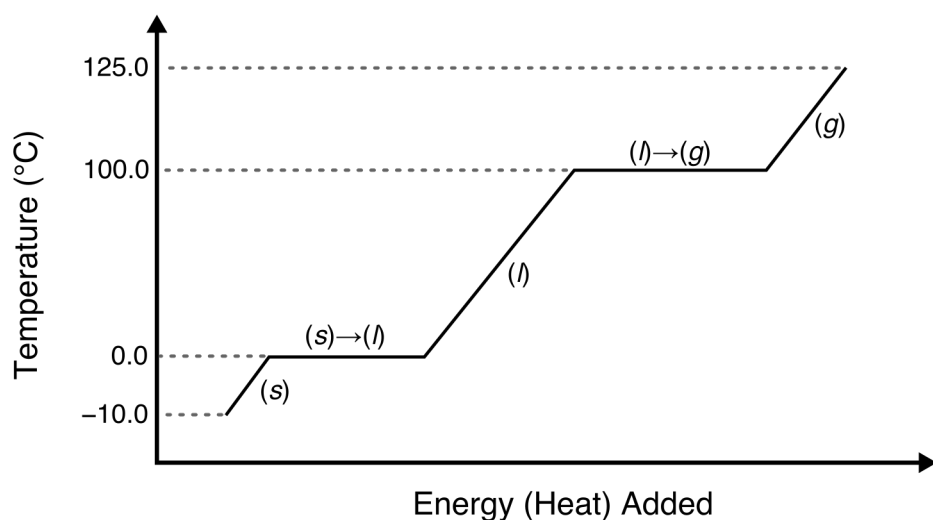
$$n_{\text{H}_2\text{O}} = 5.00 \text{ g H}_2\text{O} \times \frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}} = 0.277_5 \text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$  =  $102.9\text{ J}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$

$$\begin{aligned}
 q_2 &= n\Delta H_{\text{fus}} \\
 &= (0.277_5\text{ mol}) \left( 6.01 \frac{\text{kJ}}{\text{mol}} \right) \\
 q_2 &= 1.66_8\text{ kJ} = 166_8\text{ J}
 \end{aligned}$$

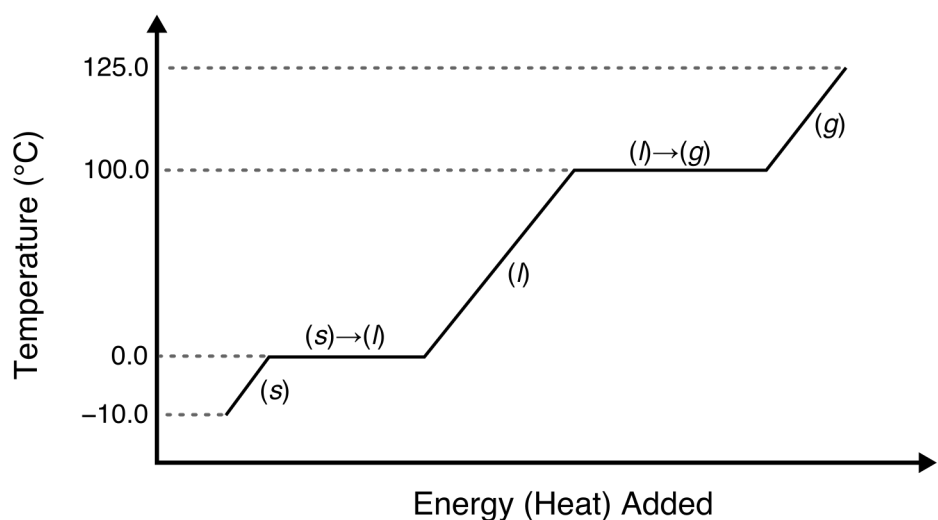
$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1 =$  heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C} = 102.9\text{ J}$
- $q_2 =$  changing all ice to water at  $0.0\text{ }^{\circ}\text{C} = 166_8\text{ J}$
- $q_3 =$  heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$

$$q_3 = nc_p\Delta T$$

$$= (0.277_5\text{ mol}) \left( 75.3 \frac{\text{J}}{\text{mol} \cdot ^{\circ}\text{C}} \right) (100.0\text{ }^{\circ}\text{C} - 0.0^{\circ}\text{C})$$

$$q_3 = 208_9\text{ J}$$

$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

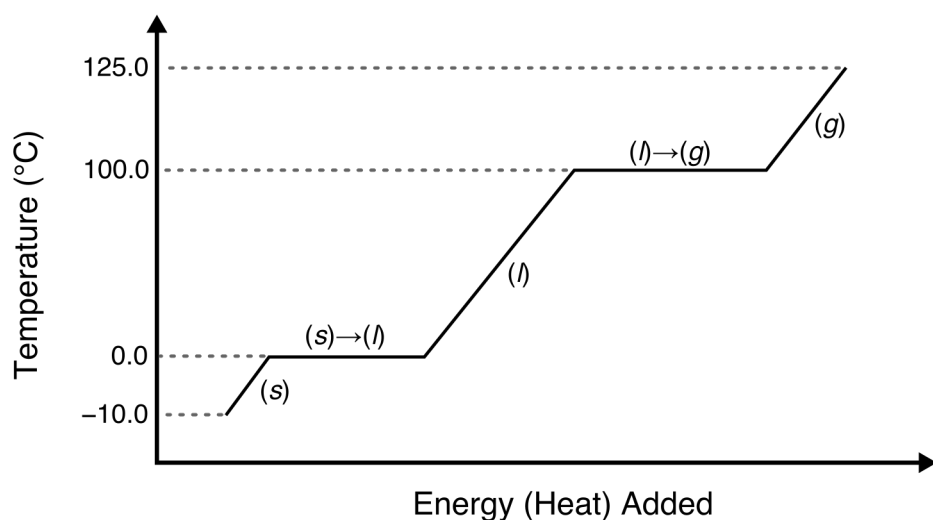


## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$  =  $102.9\text{ J}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$  =  $166_8\text{ J}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$  =  $208_9\text{ J}$
- $q_4$  = changing all water to vapor at  $100.0\text{ }^{\circ}\text{C}$

$$q_4 = n\Delta H_{\text{vap}}$$

$$= (0.277_5\text{ mol}) \left( 40.67 \frac{\text{kJ}}{\text{mol}} \right)$$

$$q_4 = 11.2_8\text{ kJ} = 112_84\text{ J}$$

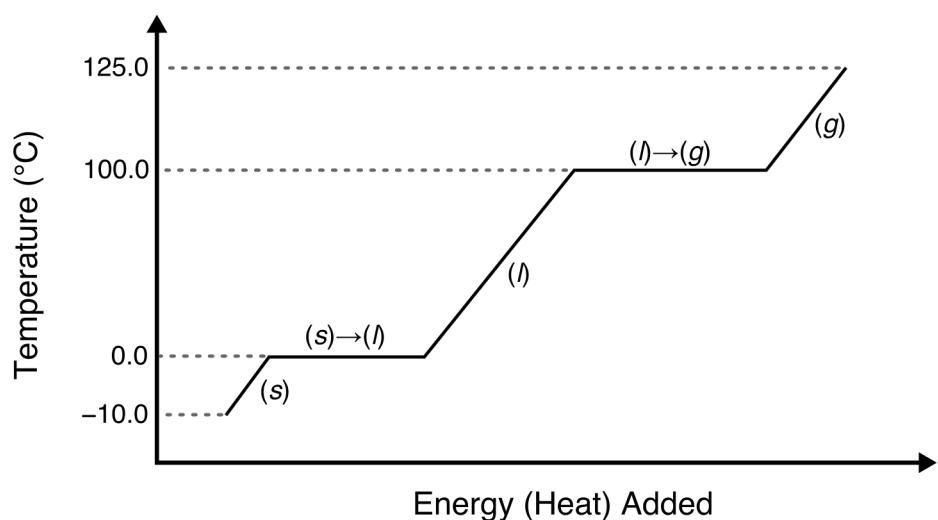
$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1 =$  heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C} = 102.9\text{ J}$
- $q_2 =$  changing all ice to water at  $0.0\text{ }^{\circ}\text{C} = 166_8\text{ J}$
- $q_3 =$  heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C} = 208_9\text{ J}$
- $q_4 =$  changing all water to vapor at  $100.0\text{ }^{\circ}\text{C} = 112_{84}\text{ J}$
- $q_5 =$  heating vapor from  $100.0\text{ }^{\circ}\text{C}$  to  $125.0\text{ }^{\circ}\text{C}$

$$q_5 = nc_p\Delta T$$

$$= (0.277_5\text{ mol}) \left( 33.6 \frac{\text{J}}{\text{mol} \cdot ^{\circ}\text{C}} \right) (125.0\text{ }^{\circ}\text{C} - 100.0\text{ }^{\circ}\text{C})$$

$$q_5 = 233.1\text{ J}$$

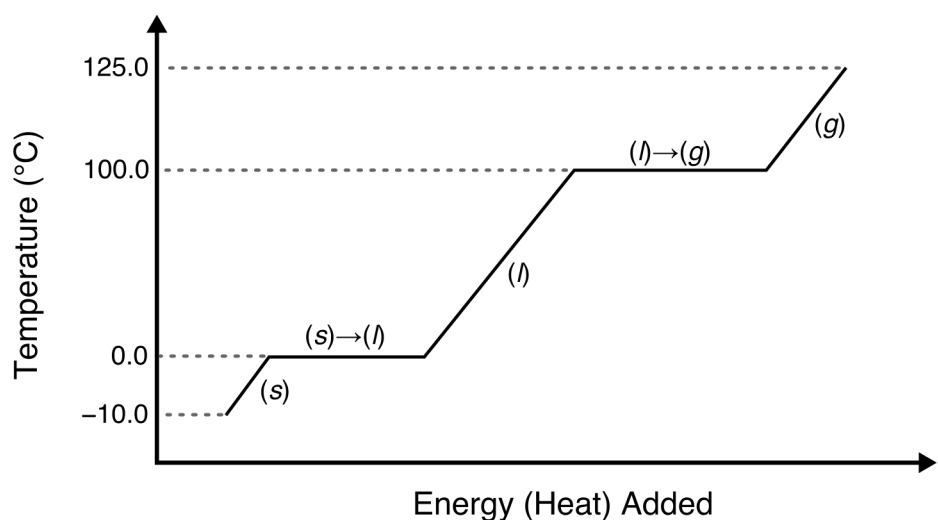
$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1 =$  heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C} = 102.9\text{ J}$
- $q_2 =$  changing all ice to water at  $0.0\text{ }^{\circ}\text{C} = 166_8\text{ J}$
- $q_3 =$  heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C} = 208_9\text{ J}$
- $q_4 =$  changing all water to vapor at  $100.0\text{ }^{\circ}\text{C} = 112_{84}\text{ J}$
- $q_5 =$  heating vapor from  $100.0\text{ }^{\circ}\text{C}$  to  $125.0\text{ }^{\circ}\text{C} = 233.1\text{ J}$

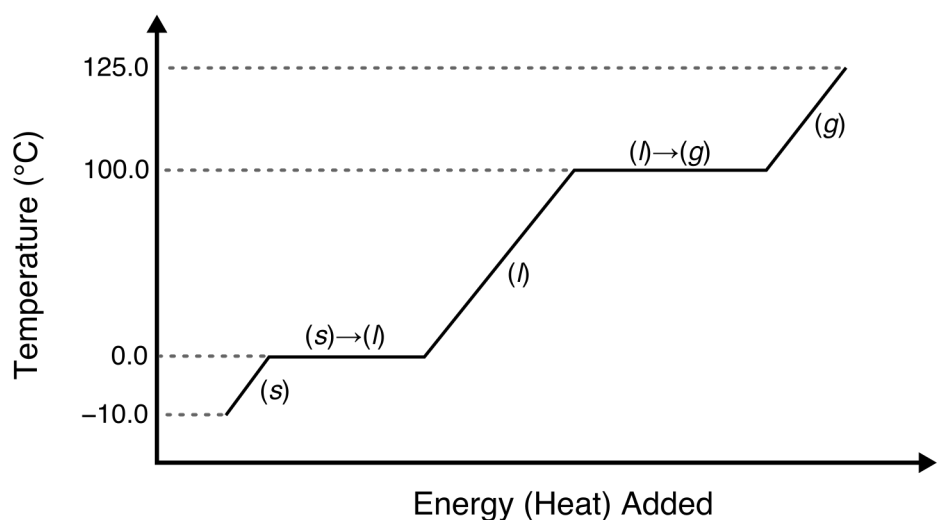
$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$

## A Guided Example

Say we have a 5.00 g block ice at  $-10.0\text{ }^{\circ}\text{C}$ .

How much heat does it take to convert this entire mass of ice into water vapor at  $125.0\text{ }^{\circ}\text{C}$ ?

We can plot the temperature of the system as a function of energy (heat) added:



The sloped regions are heating of a particular phase.

The horizontal regions are where we change phases.

There are five total heating regions:

- $q_1$  = heating ice from  $-10.0\text{ }^{\circ}\text{C}$  to  $0.0\text{ }^{\circ}\text{C}$  =  $102.9\text{ J}$
- $q_2$  = changing all ice to water at  $0.0\text{ }^{\circ}\text{C}$  =  $166_8\text{ J}$
- $q_3$  = heating water from  $0.0\text{ }^{\circ}\text{C}$  to  $100.0\text{ }^{\circ}\text{C}$  =  $208_9\text{ J}$
- $q_4$  = changing all water to vapor at  $100.0\text{ }^{\circ}\text{C}$  =  $112_{84}\text{ J}$
- $q_5$  = heating vapor from  $100.0\text{ }^{\circ}\text{C}$  to  $125.0\text{ }^{\circ}\text{C}$  =  $233.1\text{ J}$

$$q_{\text{total}} = q_1 + q_2 + q_3 + q_4 + q_5$$

$$q_{\text{total}} = 15400\text{ J} = 15.4\text{ kJ}$$

$$n_{\text{H}_2\text{O}} = 5.00\text{ g H}_2\text{O} \times \frac{1\text{ mol H}_2\text{O}}{18.02\text{ g H}_2\text{O}} = 0.277_5\text{ mol H}_2\text{O}$$