

Freezing Point Depression Boiling Point Elevation

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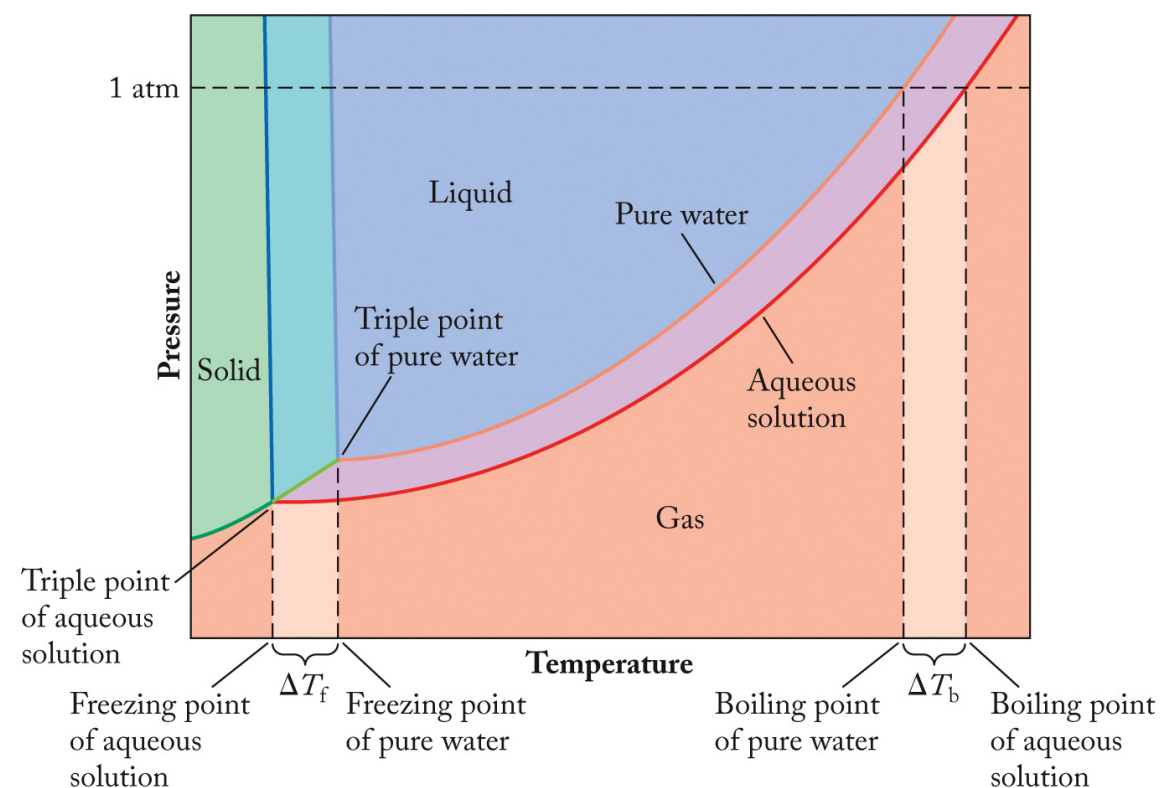
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In general, adding solute to a solvent (i.e., creating a solution) has two effects:

1. Elevates the boiling point
2. Depresses the melting point



QUANTIFYING COLLIGATIVE PROPERTIES

To determine the change in freezing point or boiling point of a solution, we use the following two equations, respectively:

FREEZING POINT DEPRESSION

$$\Delta T_f = iK_f m$$

BOILING POINT ELEVATION

$$\Delta T_b = iK_b m$$

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ΔT_f or ΔT_b = change in temperature ($^{\circ}\text{C}$)

i = number of dissociated particles per mole of solute

K_f or K_b = constant values ($^{\circ}\text{C}/m$)

m = molality (mol/kg or m)

$$m = \frac{n_{\text{solute}}}{\text{kg solvent}}$$

Determine the change in boiling point of a solution made by dissolving 125 mg of $C_{10}H_{14}O$ in 1.50 g of CS_2 ($K_b = 2.34 \text{ }^\circ\text{C}/m$).

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Your first actual step in these types of problem is to determine what kind of compound you have! Because:

- Molecular compounds that dissolve have an $i = 1$ since they do not dissociate.
- Insoluble ionic compounds do **not** dissociate in water, so **no changes** are observed!
- Soluble ionic compounds have theoretical i values equal to the number of ions per mole compound.

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Step two is to find the molality of your solution:

$$m = \frac{n_{\text{solute}}}{\text{kg solvent}} = \frac{125 \text{ mg } C_{10}H_{14}O \times \frac{1 \text{ g}}{1000 \text{ mg}} \times \frac{1 \text{ mol } C_{10}H_{14}O}{150.21 \text{ g}}}{1.50 \text{ g } CS_2 \times \frac{1 \text{ kg}}{1000 \text{ g}}} = 0.555 \text{ } m$$

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And finally solve for the change in boiling point:

$$\begin{aligned}\Delta T_b &= iK_b m \\ &= (1) \left(2.34 \frac{^\circ\text{C}}{m} \right) (0.555 \text{ } m) \\ &= 1.30 \text{ } ^\circ\text{C}\end{aligned}$$

The freezing point of an aqueous solution ($K_f = 1.86 \text{ }^\circ\text{C}/m$) with a molality of $0.0935 \text{ } m$ ammonium chloride is $-0.322 \text{ }^\circ\text{C}$.
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$$\begin{aligned}\Delta T_f &= iK_fm \\ -0.322 \text{ }^\circ\text{C} &= i \left(1.86 \frac{^\circ\text{C}}{m} \right) (0.0935 \text{ } m) \\ i &= 1.85\end{aligned}$$

The freezing point of an aqueous solution ($K_f = 1.86 \text{ }^\circ\text{C}/m$) of ammonium sulfate is $-0.173 \text{ }^\circ\text{C}$, where $i = 2.46$.

What mass of ammonium sulfate did we start with if the volume of water is 10.0 L?

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$$\begin{aligned}\Delta T_f &= iK_fm \\ -0.173 \text{ }^\circ\text{C} &= (2.46) \left(1.86 \frac{^\circ\text{C}}{m} \right) (m) \\ m &= 0.0378\end{aligned}$$

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We can then extract the mass from the molality:

$$\begin{aligned}0.0378 m &= \frac{n_{\text{solute}}}{10.0 \text{ L H}_2\text{O} \times \frac{1000 \text{ mL}}{1 \text{ L}} \times \frac{1 \text{ g}}{1 \text{ mL}} \times \frac{1 \text{ kg}}{1000 \text{ g}}} \\ n_{\text{solute}} &= 0.378 \text{ mol } (\text{NH}_4)_2\text{SO}_4\end{aligned}$$

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