



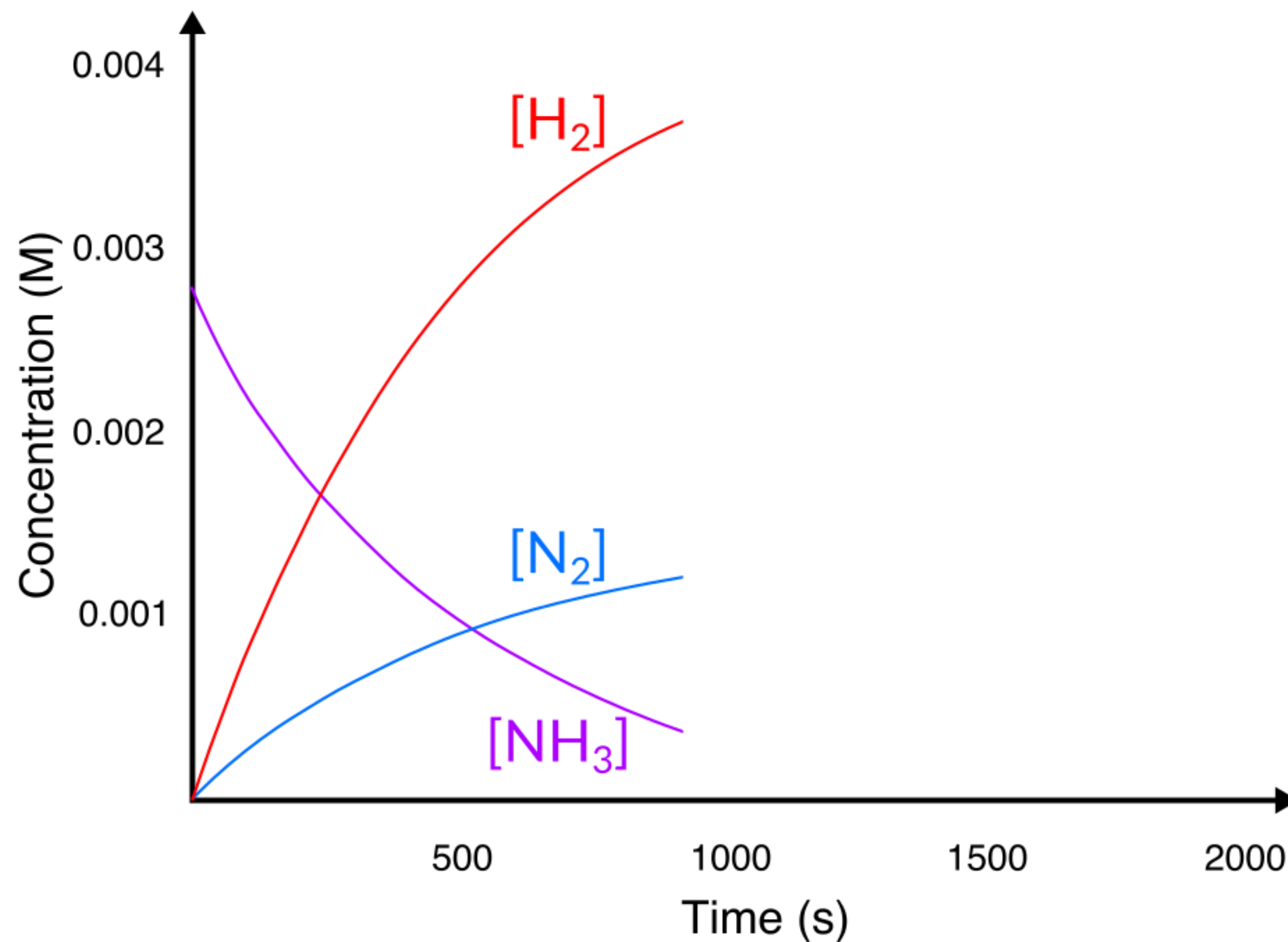
EQUILIBRIUM

INTRODUCTION: DEFINITIONS AND K VALUES

CHEMISTRY 165 // SPRING 2020

Chemical equilibrium

Consider the decomposition of ammonia gas into nitrogen gas and hydrogen gas.

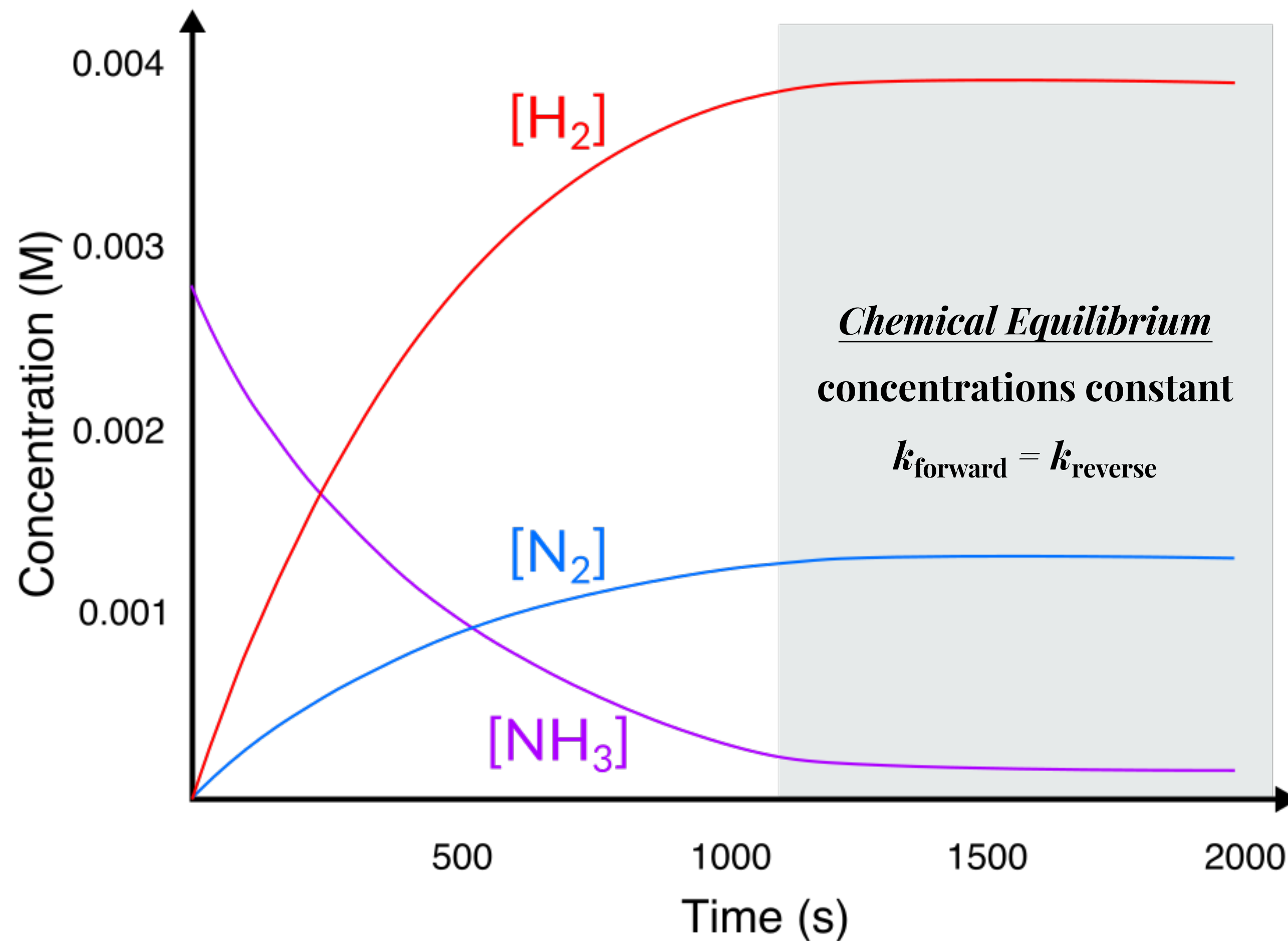


Notice the arrow is unidirectional (\rightarrow), which indicates the reaction proceeds in the direction to the right. This coincides with the plot of the concentrations over time since $[\text{H}_2]$ and $[\text{N}_2]$ increase and $[\text{NH}_3]$ decreases over time.

But what if we waited longer?

Chemical equilibrium

Consider the decomposition of ammonia gas into nitrogen gas and hydrogen gas.



But what if we waited longer?

The concentrations would plateau rather than go to zero for the reactants. At this point, we reach chemical equilibrium. This is a dynamical process where NH₃ continues to decompose, but N₂ and H₂ will also re-combine to form NH₃ again. And the rates at which these forward and reverse processes occur are equal to each other.

$$k_{\text{forward}} = k_{\text{reverse}}$$

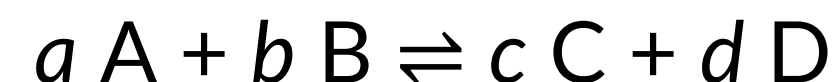
To better represent the dynamic nature of chemical reactions that reach equilibrium we use the \rightleftharpoons arrow to indicate both processes occurring.



Quantifying equilibrium: K_c values

As it turns out, regardless of what initial conditions (concentrations) we start with we always end up at equilibrium. This behavior means suggests that we can express equilibrium quantitatively through an equilibrium constant (K).

Consider the general balanced chemical equation:



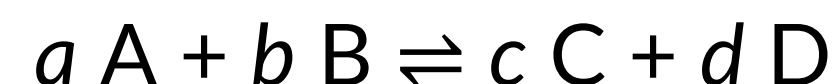
The equilibrium constant for this reaction is expressed using the Law of Mass Action and is a ratio between the amount of products to reactants:

The diagram illustrates the equilibrium constant equation $K_c = \frac{[C]^c [D]^d}{[A]^a [B]^b}$ with three explanatory text boxes and arrows:

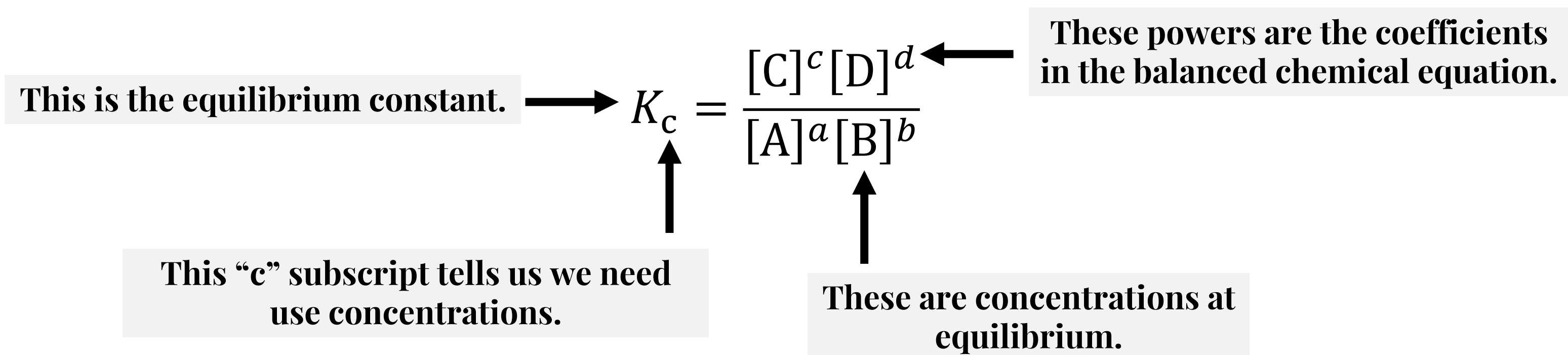
- A box on the left: "This is the equilibrium constant." with an arrow pointing to K_c .
- A box below the numerator: "This 'c' subscript tells us we need use concentrations." with an arrow pointing to the exponent c .
- A box below the denominator: "These are concentrations at equilibrium." with an arrow pointing to the concentration terms $[A]^a [B]^b$.
- A box on the right: "These powers are the coefficients in the balanced chemical equation." with an arrow pointing to the exponents c and d .

Quantifying equilibrium: K_p values

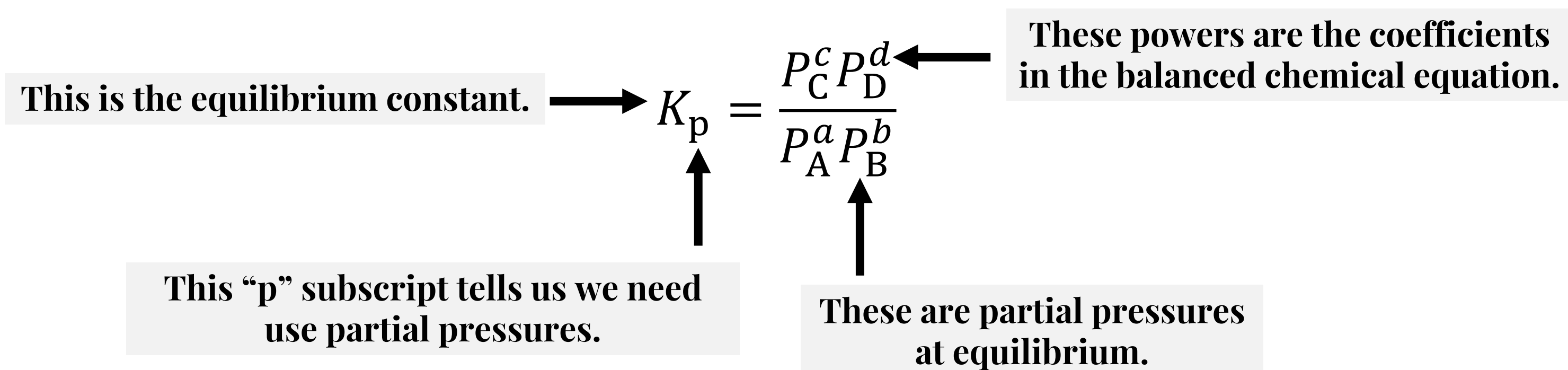
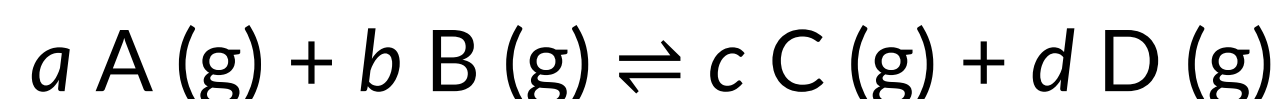
Consider the general balanced chemical equation:



The equilibrium constant for this reaction is expressed using the Law of Mass Action and is a ratio between the amount of products to reactants:



If the equilibrium were among only gases, we could also write another equilibrium constant:



Features of K_c and K_p

Despite the forms of the equilibrium constants, they are unitless/dimensionless quantities.

Additionally, for gaseous equilibria we can convert between K_c and K_p via the ideal gas law to re-express partial pressures in terms of concentrations. Here I show it for a gas compound C.

$$P_C V = n_C RT$$

$$P_C = \frac{n_C}{V} RT$$

$$P_C = [C] RT$$

Now, we can substitute our partial pressures in the K_p expression for concentrations and derive the relationship between K_c and K_p :

$$K_p = \frac{P_C^c P_D^d}{P_A^a P_B^b} = \frac{([C]RT)^c ([D]RT)^d}{([A]RT)^a ([B]RT)^b} = \underbrace{\frac{[C]^c [D]^d}{[A]^a [B]^b}}_{\text{This is } K_c!} \cdot \frac{(RT)^{c+d}}{(RT)^{a+b}} = K_c \cdot (RT)^{\Delta n}$$

Remember these powers are just the coefficients in the balanced chemical equation, so:

$$\Delta n = (c + d) - (a + b)$$

This Δn is just the change in the number of moles of products and reactants!

Manipulating K values

Because the K values are written based on the balanced chemical equation, K values can be different depending on how you balance the equation.

For instance, consider the three balanced chemical equations and their K_c values at 425 K.

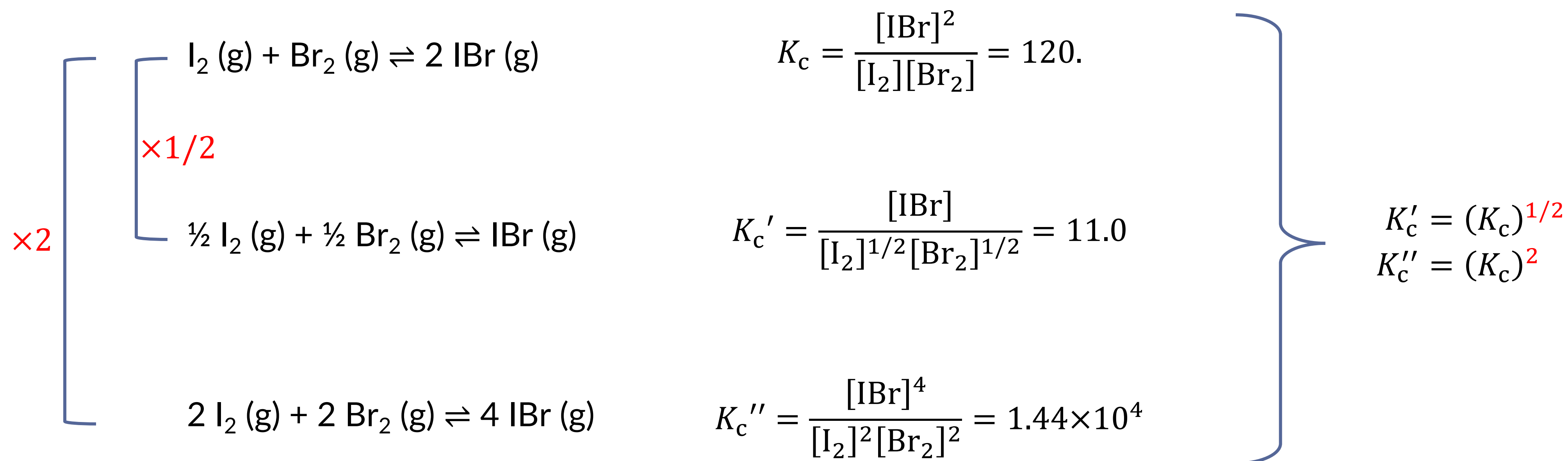


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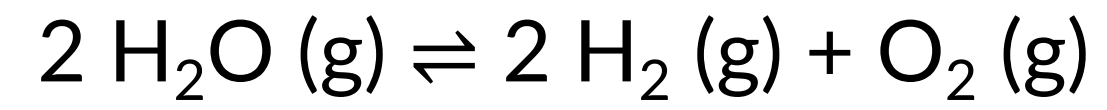
For instance, consider the three balanced chemical equations and their K_c values at 425 K.

Luckily, the relationship between the different K_c values is just related to the **quantity (n)** by which we multiple the first balanced equation. The other K_c values are simply mathematical manipulations of K_c^n .



PRACTICE PROBLEM 1

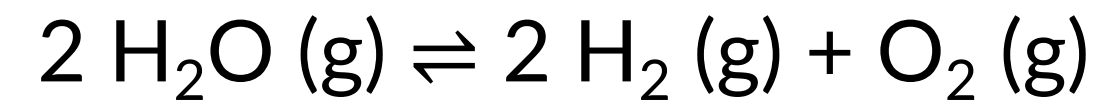
At 1200 K, the partial pressures of an equilibrium mixture of H₂O, H₂, and O₂ gases are 0.040, 0.0045, and 0.0030 atm, respectively. Calculate the value of the equilibrium constant K_p for the reaction at 1200 K.



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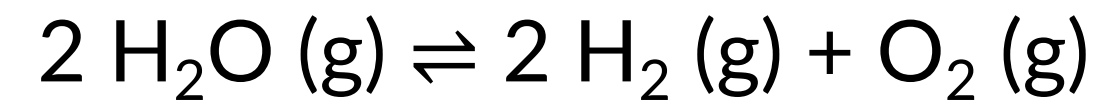


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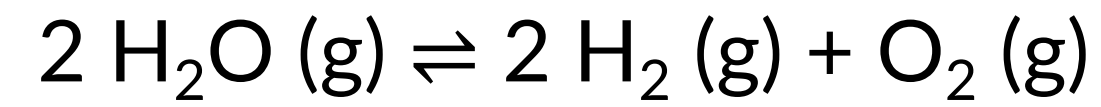
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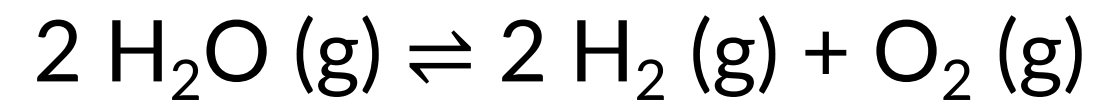
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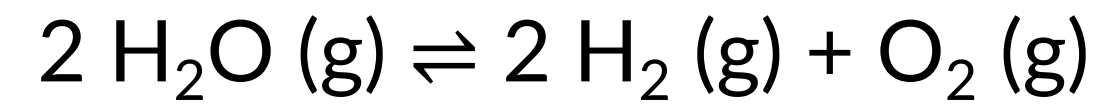
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$$\begin{aligned} K_p &= \frac{P_{\text{H}_2}^2 P_{\text{O}_2}}{P_{\text{H}_2\text{O}}^2} \\ &= \frac{(0.0045)^2 (0.0030)}{(0.040)^2} \\ K_p &= 3.8 \times 10^{-5} \end{aligned}$$

PRACTICE PROBLEM 2

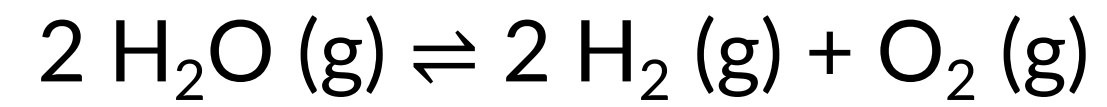
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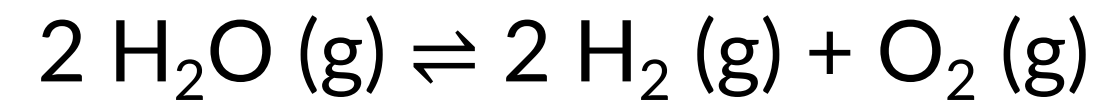
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Start from the K_p expression.

$$K_p = 3.7_9 \times 10^{-5}$$

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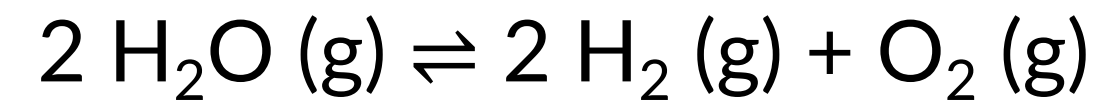
$$K_p = 3.79 \times 10^{-5}$$

We can convert from K_p to K_c via:

$$K_p = K_c(RT)^{\Delta n}$$

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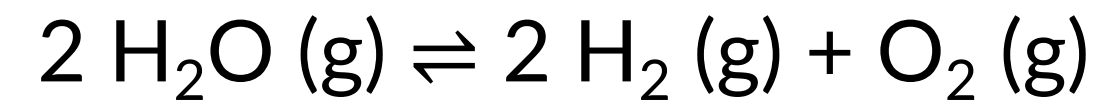
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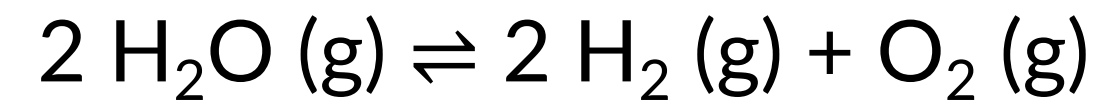
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$$K_p = K_c(RT)^{\Delta n}$$
$$3.7_9 \times 10^{-5} = K_c(0.08206 \times 1200)^1$$

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$$\begin{aligned} K_p &= K_c(RT)^{\Delta n} \\ 3.79 \times 10^{-5} &= K_c(0.08206 \times 1200)^1 \\ K_c &= 3.9 \times 10^{-7} \end{aligned}$$

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PRACTICE PROBLEM 3

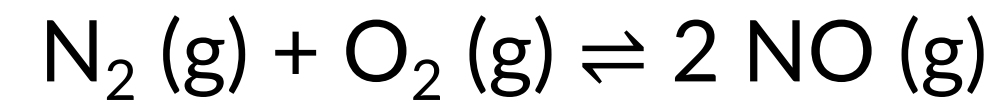
At equilibrium, the concentrations of gaseous N_2 , O_2 , and NO in a container are $[\text{N}_2] = 3.3 \text{ M}$, $[\text{O}_2] = 5.8 \text{ M}$, and $[\text{NO}] = 3.1 \text{ M}$. Calculate the value of K_c for this reaction.



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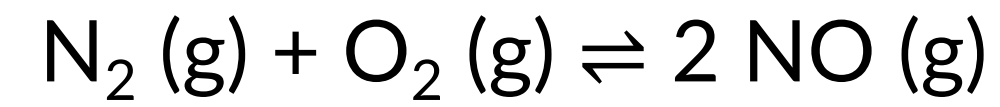


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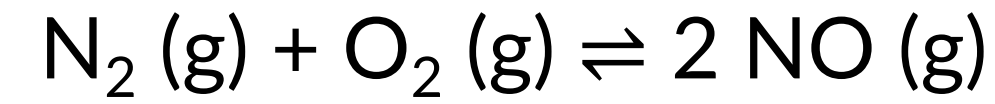
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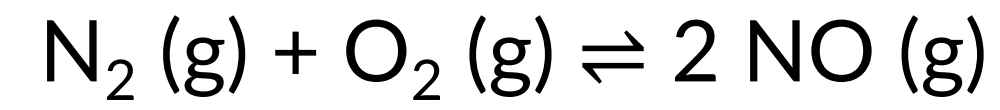
Next, we can calculate the equilibrium constant by inserting the equilibrium concentrations given to us.

$$\begin{aligned} K_c &= \frac{[\text{NO}]^2}{[\text{N}_2][\text{O}_2]} \\ &= \frac{(3.1)^2}{(3.3)(5.8)} \\ K_c &= 0.50 \end{aligned}$$

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At equilibrium, the concentrations of gaseous N_2 , O_2 , and NO in a container are $[\text{N}_2] = 3.3 \text{ M}$, $[\text{O}_2] = 5.8 \text{ M}$, and $[\text{NO}] = 3.1 \text{ M}$.

Calculate the value of K_c for this reaction. **What is the equilibrium constant for the reverse reaction?**

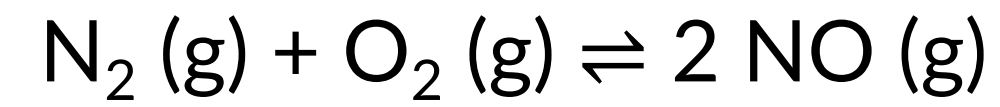


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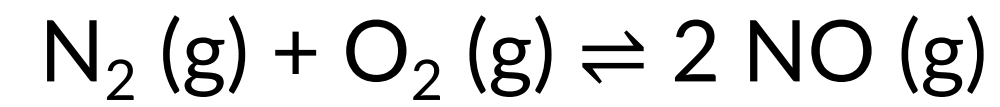
Recognize that the reverse process would be:



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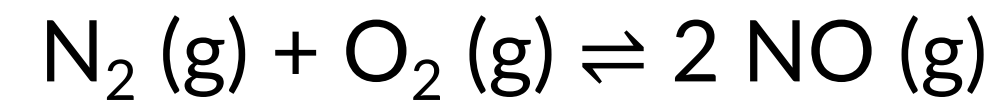
The equilibrium expression for this would be:

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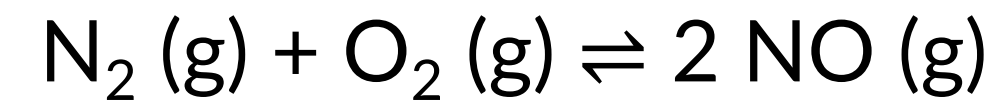


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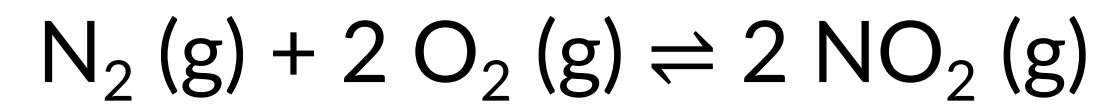
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Understand that the relationship between the forward and reverse K expression is simply:

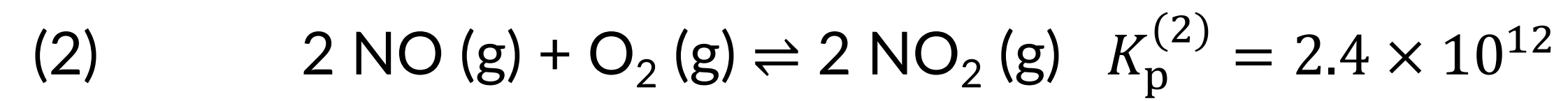
$$K_c^{\text{reverse}} = \frac{1}{K_c^{\text{forward}}}$$

PRACTICE PROBLEM 5

Calculate the value of K_p at 298 K for the reaction



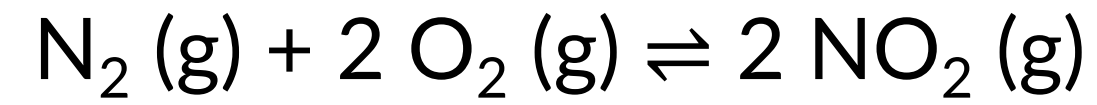
From the following two K_p values at 298K.



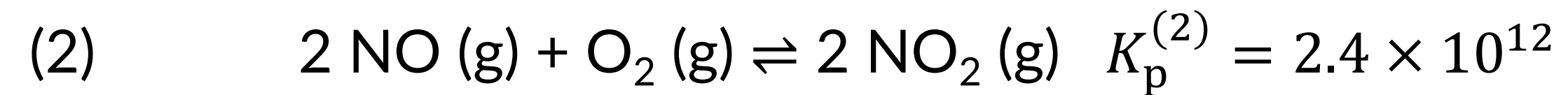
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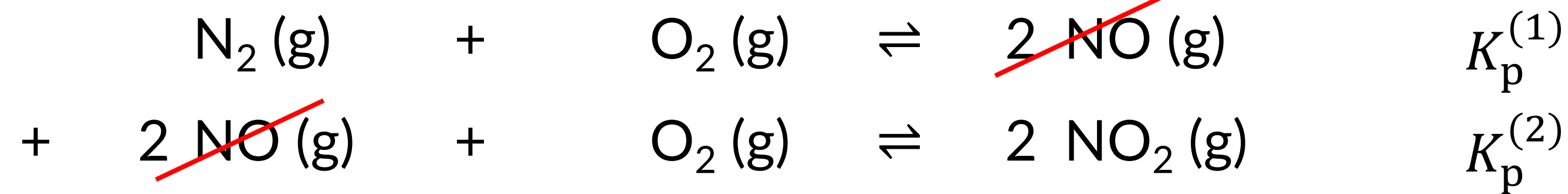


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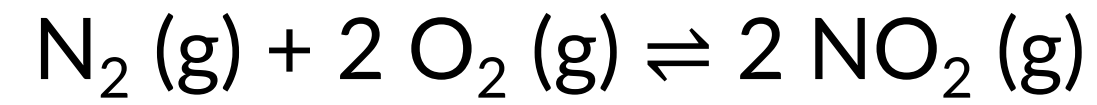
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Similar to Hess's Law, we can combine equations (1) and (2) together.

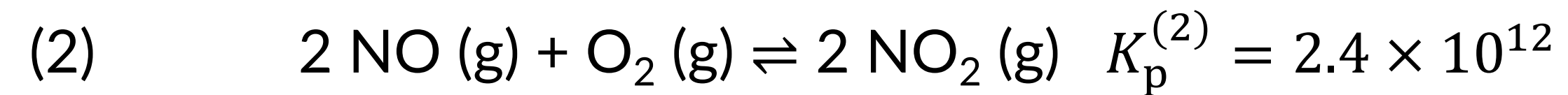


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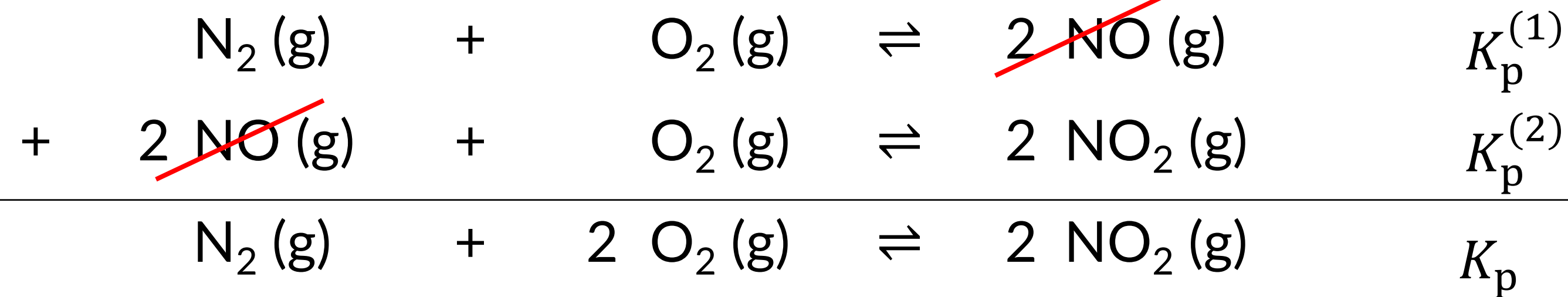


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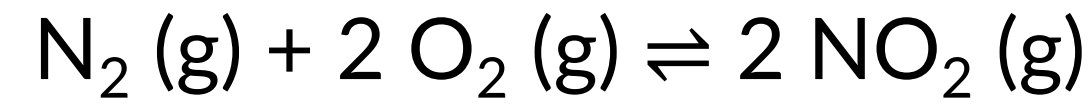
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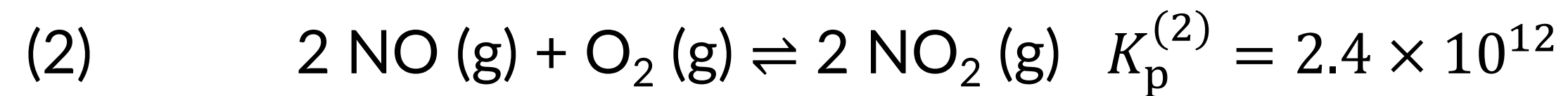


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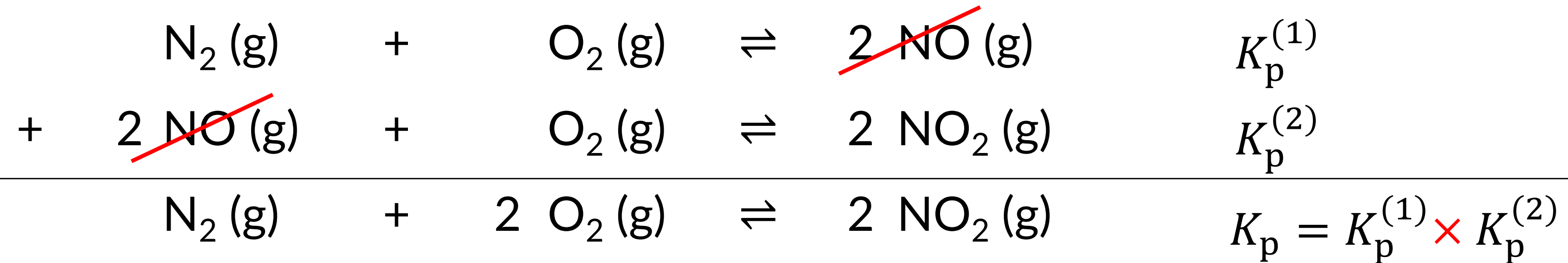


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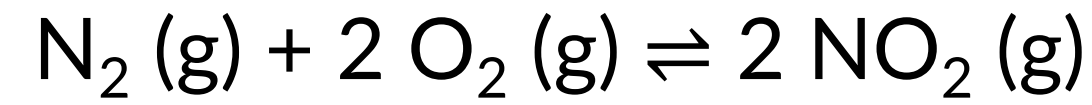
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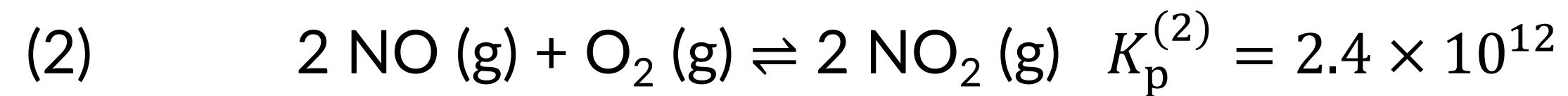


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